REFERENCE LIST FOR STATE-OF-ART SURVEY OF FRACTIONAL ORDER MODELING AND ESTIMATION METHODS FOR LITHIUM-ION BATTERIES

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This paper is dedicated to the memory of late Professor Wen Chen

This is only the reference list of "STATE-OF-ART SURVEY OF FRACTIONAL ORDER MODELING AND ESTIMATION METHODS FOR LITHIUM-ION BATTERIES".

The list is provided to readers for easier look-up of the cited papers in the survey paper.

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