Containment Control of Fractional Order Multi-Agent Systems with Time Delays
Hongyong Yang, Fuyong Wang and Fujun Han

Abstract—In complex environments, many distributed multi-agent systems are described with the fractional-order dynamics. In this paper, containment control of fractional-order multi-agent systems with multiple leader agents are studied. Firstly, the collaborative control of fractional-order multi-agent systems (FOMAS) with multiple leaders is analyzed in a directed network without delays. Then, by using Laplace transform and frequency domain theorem, containment consensus of networked FOMAS with time delays is investigated in an undirected network, and a critical value of delays is obtained to ensure the containment consensus of FOMAS. Finally, numerical simulations are shown to verify the results.

Index Terms—containment control, multi-agent systems, fractional-order, time delays.

I. INTRODUCTION

RECENTLY, with the rapid development of network and communication technology, the distributed coordination for networked systems has been studied deeply ([1–5]). Cooperative control of multi-agent systems has become a hot topic in the fields of automation, mathematics, computer science, etc ([6–10]). It has been applied in both military and civilian sectors, such as the formation control of mobile robots, the cooperative control of unmanned spacecraft, the attitude adjustment and position of satellite, and the scheduling of smart power grid systems, etc. As a kind of distributed cooperative control problems of multi-agent systems with multiple leaders, containment control regulates followers eventually converge to a target area (convex hull formed by the leaders) by designing a control protocol, which has been paid much more attention in recent years ([11–13]).

In the complex practical environments, many distributed systems cannot be illustrated with the integer-order dynamics and can only be characterized with the fractional-order dynamics ([14–16]). For example, flocking movement and food searching by means of the individual secrections, exploring of submarines and underwater robots in the seabed with a massive number of microorganisms and viscous substances, working of unmanned aerial vehicles in the complex space environment ([17–18]). Cao and Ren have studied the coordination of multi-agent systems with fractional order ([19–20]), and obtained the relationship between the number of individuals and the order in the stable fractional system. Yang et.al have studied the distributed coordination of fractional order multi-agent systems with communication delays ([21–22]). Motivated by the broad application of coordination algorithms in FOMAS, the containment control of distributed fractional-order systems will be studied in this paper.

For containment control problems, the current research works are mainly focused on integer-order systems ([11–13,23–26]). In [11], containment control problem for first-order multi-agent systems with the undirected connected topology is investigated, and the effectiveness of control strategy is proven by using partial differential equation method. In [12], second-order multi-agent systems with multiple leaders are investigated, the containment control of multi-agent systems with multiple stationary leaders can be achieved in arbitrary dimensions. In [13], two asymptotic containment controls of continuous-time systems and discrete-time systems are proposed for the multi-agent systems with dynamic leaders, and the constraint condition for control gain and sampling period are given. Considering factors such as external disturbance and parameter uncertainty in [23], the attitude containment control problem of nonlinear systems are studied in a directed network. The impulsive containment control for second-order multi-agent systems with multiple leaders is studied in [25–26], where all followers are regulated to access the dynamic convex hull formed by the dynamic leaders.

When agents transfer information by means of sensors or other communication devices in coordinated network, communication delays have a great impact on the behaviors of the agents. Now, the influences of communication delays on multi-agent systems have also been paid more attentions ([2,7–10]) where these research activities on the coordination problem are mainly concentrated on integer-order multi-agent systems. In [24], containment control problem of multi-agent systems with time delays is studied in fixed topology, and two cases of multiple dynamic leaders and multiple stationary leaders are discussed, respectively. As far as we know, few researches have been done on the containment consensus of fractional order multi-agent systems with time delays.

In this paper, the containment control algorithms for multi-agent systems with fractional dynamics are presented, and the containment consensus of distributed FOMAS with communication delays is studied under directed connected topologies. The main innovation of this paper is that the distributed containment control of fractional order multi-agent systems with multiple leaders and communication delays is studied for the first time. The research presented in this paper is different from Reference [21], where consensus of FOMAS without lea-

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der[21] is much easier than containment control of FOMAS with multiple leaders in this paper. The rest of the paper is organized as follows. In Section 2, we recall some basic definitions about fractional calculus. In Section 3, some preliminaries about graph theory are shown, and fractional order coordination model of multi-agent systems is presented. Containment control of fractional coordination algorithm for multi-agent systems with communication delay is studied in Section 4. In Section 5, numerical simulations are used to verify the theoretical analysis. Conclusions are finally drawn in Section 6.

II. FRACTIONAL CALCULUS

Fractional calculus has played an important role in modern science. There are two fractional operators used widely: Caputo and Riemann-Liouville (R-L) fractional operators. In physical systems, Caputo fractional order operator is more practical than R-L fractional order operator because R-L operator has initial value problems. Therefore, in this paper we will apply Caputo fractional order operator to describe the system dynamics and analyze the stability of proposed FOMAS algorithms. Generally, Caputo operator includes Caputo fractional integral and Caputo fractional derivative. Caputo fractional integral is defined as

\[
\mathcal{C}_0^\alpha \int_0^t f(t) \, dt = \frac{1}{\Gamma(p)} \int_0^t \frac{f(\theta)}{(t-\theta)^{1-p}} \, d\theta,
\]

where the integral order \( p \in (0, 1] \), \( \Gamma(.) \) is the Gamma function, and \( t_0 \) is a real number. Based on the Caputo fractional integral, for a nonnegative real number \( \alpha \), Caputo fractional derivative is defined as

\[
\mathcal{C}_0^\alpha \frac{d^p}{dt^p} f(t) = \mathcal{C}_0^\alpha \frac{d^\alpha}{dt^\alpha} f(t) = \mathcal{C}_0^\alpha \int_0^t \frac{d^{[\alpha]+1}}{d(t-\theta)^{[\alpha]+1}} f(t) \, d\theta,
\]

where \( p = [\alpha] + 1 - \alpha \in (0, 1] \) and \( [\alpha] \) is the integral part of \( \alpha \). If \( \alpha \) is an integer, then \( p = 1 \) and the Caputo fractional derivative is equivalent to the integer-order derivative. In this paper, we will use a simple notation \( f^{(\alpha)} \) to replace \( \mathcal{C}_0^\alpha f(t) \).

Let \( \mathcal{L}(\cdot) \) denote the Laplace transform of a function, the Laplace transform of Caputo derivative is shown as

\[
\mathcal{L}(f^{(\alpha)})(s) = s^\alpha F(s) - \sum_{k=1}^{[\alpha]+1} s^{\alpha-1} f^{(k-1)}(0),
\]

where \( F(s) = \mathcal{L}(f(t)) = \int_0^\infty e^{-st} f(t) \, dt \) is the Laplace transform of function \( f(t) \), \( f^{(k)}(0) = \lim_{\xi \to 0-} f^{(k)}(\xi) \) and \( f^{(0)} = f(0) = \lim_{\xi \to 0-} f(\xi) \).

III. PROBLEM STATEMENT

Assume that \( n \) autonomous agents constitute a network topology graph \( G = (V, E, A) \), in which \( V = \{v_1, v_2, ..., v_n\} \) represents a set of \( n \) nodes, and its edges set is \( E \subseteq V \times V \). \( I = \{1, 2, ..., n\} \) is the node indexes set, \( A = [a_{ij}] \in \mathbb{R}^{n \times n} \) is an adjacency matrix with elements \( a_{ij} \geq 0 \). An edge of the diagraph \( G \) is denoted by \( e_{ij} = (v_i, v_j) \in E \). Let the adjacency element \( a_{ij} > 0 \) when \( e_{ij} \in E \), otherwise, \( a_{ij} = 0 \). The neighbors’ set of node \( i \) is denoted by \( N_i = \{j \in I : a_{ij} > 0\} \).

Let \( G \) be a weighted graph without self-loops, i.e., \( a_{ii} = 0 \), and matrix \( D = \text{diag}\{d_1, d_2, ..., d_n\} \) be the diagonal matrix with the diagonal elements \( d_i = \sum_{j=1}^n a_{ij} \) representing the out-degree of the \( i \)-th agent. \( L = D - A \) is the Laplacian matrix of the weighted digraph \( G \). For two nodes \( i \) and \( k \), there is index set \( \{k_1, k_2, ..., k_l\} \) satisfying \( a_{ik} > 0, a_{kj} > 0, \ldots, a_{k_lk} > 0 \), then there is an information transmission linked path between node \( i \) and \( k \), also we say node \( i \) can transfer the information to node \( k \). If node \( i \) can find a path to reach any node of the graph, then node \( i \) is globally reachable from every other node in the digraph.

Lemma 1[5]. 0 is a simple eigenvalue of Laplacian matrix \( L \), and \( X_0 = [1, 1, ..., 1]^T \) is corresponding right eigenvector, i.e., \( LX_0 = 0 \), if and only if the digraph \( G = (V, E, A) \) has a globally reachable node.

Lemma 2[6]. Matrix \( L + B \) is a positive definite matrix, where \( L \) is a Laplacian matrix of the digraph \( G = (V, E, A) \) with a globally reachable node, and \( B = \text{diag}\{b_1, ..., b_n\} \) with \( b_i > 0 \) and at least there is one element \( b_i > 0 \).

Definition 1. The convex hull of a finite set of points \( x_1, ..., x_m \) denoted by \( Co\{x_1, ..., x_m\} \), is the minimal convex set containing all points \( x_i, i = 1, ..., m \). More specifically, \( Co\{x_1, ..., x_m\} = \{\sum_{i=1}^m \nu_i x_i | \nu_i > 0, \sum_{i=1}^m \nu_i = 1\} \).

Recently, Fractional order systems have been widely applied in various science fields, such as physics, hydrodynamics, biophysics, aerodynamics, signal processing and modern control. The theories of fractional order equations are studied deeply, and the relationship between the fractional order and the number of agents to ensure coordination has been presented in [19]. Assume that Caputo fractional derivative is used to indicate the dynamics of multi-agent systems in the complex environments, the fractional order dynamical equations are defined as:

\[
x_i^{(\alpha)}(t) = u_i(t), i = 1, ..., n,
\]

where \( x_i(t) \in R \) and \( u_i(t) \in R \) represent the \( i \)-th agent’s state and control input respectively, \( x_i^{(\alpha)} \) represents the \( \alpha \)-order Caputo derivative. Assume the following control protocols are used in FOMAS:

\[
u_i(t) = -\gamma \sum_{k \in N_i} a_{ik} [x_i(t) - x_k(t)], i \in I.
\]

where \( a_{ik} \) represents the \((i, k)\) elements of adjacency matrix \( A \), \( \gamma > 0 \) is control gain, \( N_i \) represents the neighbors collection of the \( i \)-th agent.

Suppose the multi-agent systems consisting of \( n_1 \) following agents and \( n_2 \) leader agents in this paper, where \( n_1 + n_2 = n \). Then, the control protocols of the multi-agent systems can be rewritten as

\[
u_i(t) = \begin{cases} 
-\gamma \sum_{k \in N_i} a_{ik} [x_i(t) - x_k(t)], i = 1, 2, ..., n_1; \\
0, i = n_1 + 1, ..., n.
\end{cases}
\]

The systems(3-5) can be rewritten as

\[
X_i^{(\alpha)}(t) = -\gamma \begin{pmatrix} L_1 & L_2 \\ 0 & 0 \end{pmatrix} X(t),
\]
where $X(t) = [X_1(t), X_2(t)]^T$, $X_1(t) = [x_1(t), x_2(t), ..., x_{n_1}(t)]^T$, $X_2(t) = [x_{n_1+1}(t), ..., x_n(t)]^T$, $L_1 \in \mathbb{R}^{n_1 \times n_1}$, $L_2 \in \mathbb{R}^{n \times n_2}$. $X_1(t)$ is the set of the followers, and $X_2(t)$ is the set of the leaders.

**Remark 1.** Matrix $L_1 = (l_{ik}) \in \mathbb{R}^{n_1 \times n_1}$ satisfying

$$l_{ik} = \begin{cases} d_i - a_{ii}, & i = k, \\ -a_{ik}, & i \neq k. \end{cases}$$

Matrix $L_2 = (l_{ik}) \in \mathbb{R}^{n_1 \times n_2}$ satisfying

$$l_{ik} = -a_{ik}, \quad i = 1, 2, ..., n_1; \quad k = n_1 + 1, ..., n. \tag{8}$$

Assume the collection formed by leaders is regarded as a virtual node, if one follower agent can connect to some leader, then the follower is connected to the virtual node.

**Definition 2.** The containment control is realized for the system (3) under certain control input (5), if the position states of the followers are asymptotically converged to the convex hull formed by the leaders.

**Assumption 1.** For any one follower, there is a directed connected path to the virtual node formed by leaders.

**Lemma 3.** With Assumption 1, matrix $L_1$ is positive definite, and $-L_1^{-1}L_2$ is a non-negative matrix whose entries sum in every row equals to 1.

**Proof.** From Lemma 2, matrix $L_1$ is positive definite matrix. Let $L_1 = dI_{n_1} - Q$ where $d$ is a positive number which is large enough and matrix $Q$ is a non-negative matrix. It has

$$L_1^{-1} = (dI_{n_1} - Q)^{-1} = d^{-1}(I_{n_1} + d^{-1}Q + (d^{-1}Q)^2 + ...). \tag{9}$$

Then, we obtain $-L_1^{-1}L_2$ is a non-negative matrix.

From Lemma 1, Laplacian matrix $L$ will be satisfied with $LX_0 = 0$, where $X_0 = [1, 1, ..., 1]^T \in \mathbb{R}^{n_1 \times 1}$. Then we have

$$L_1X_{01} + L_2X_{02} = 0, \tag{10}$$

where $X_{01} = [1, 1, ..., 1]^T \in \mathbb{R}^{n_1 \times 1}$ and $X_{02} = [1, 1, ..., 1]^T \in \mathbb{R}^{n \times 1}$. Since $L_1$ is a positive definite matrix from Assumption 1 and Lemma 2, it has

$$X_{01} = -L_1^{-1}L_2X_{02}. \tag{11}$$

Therefore, $-L_1^{-1}L_2$ is a stochastic matrix with entries sum in every row equaling to 1.

**Theorem 1.** Consider a directed dynamic system of $n_1$ followers and $n_2$ leaders with dynamics (3), whose dynamic topologies are satisfied with Assumption 1. Then the containment control is realized for the FOMAS under certain control protocol (5).

**Proof.** Based on the system (6), we have

$$X_1^{(α)}(t) = -\gamma(L_1X_1(t) + L_2X_2(t)), \quad X_2^{(α)}(t) = 0. \tag{12}$$

Let $\bar{X}_1(t) = X_1(t) + L_1^{-1}L_2X_2(t)$, system (10) can be rewritten as

$$\bar{X}_1^{(α)}(t) = -\gamma L_1\bar{X}_1(t), \quad \bar{X}_2^{(α)}(t) = 0. \tag{13}$$

It is known that the fractional differential system (8) is asymptotically stable iff $\| arg(spec(L_1)) \| > \alpha\pi/2$. Since $L_1$ is positive definite matrix, $\alpha \in (0, 1]$, we obtain

$$\lim_{t \to -\infty} \bar{X}_1(t) = 0, \quad i.e. \quad \lim_{t \to -\infty} X_1(t) = -L_1^{-1}L_2X_2(t). \tag{14}$$

Since matrix $-L_1^{-1}L_2$ is stochastic matrix, the states of the followers are asymptotically converged to the convex hull formed by the leaders with Definition 1. Then, based on Definition 2, the containment control is realized for the system (3) with the control protocol (5).

**Remark 2.** If FOMAS of $n$ agents and $n_2 = 1$ leader with dynamics (3), the containment control result in Theorem 1 will become the consensus of multi-agent systems with one leader.

**Remark 3.** If the fractional order $α = 1$ in FOMAS, the containment control result in Theorem 1 will become that of multi-agent systems with integer-order dynamics.

**IV. Containment control of FOMAS with time delays**

In this section, we assume that there are communication delays in the dynamical systems, and containment control of the fractional-order agent systems with communication delays will be studied. Under the influence of communication delays, we can get the following algorithm:

$$x_i^{(α)}(t) = u_i(t - τ), \quad i = 1, ..., n, \tag{15}$$

where $τ$ is the communication delay of agent $i$. Through a simple change we can obtain

$$X_1^{(α)}(t) = -γ(L_1X_1(t - τ) + L_2X_2(t - τ)), \quad X_2^{(α)}(t) = 0. \tag{16}$$

Let $\bar{X}_1(t) = X_1(t) + L_1^{-1}L_2X_2(t)$, system (10) can be rewritten as

$$\bar{X}_1^{(α)}(t) = -γ L_1\bar{X}_1(t - τ), \quad \bar{X}_2^{(α)}(t) = 0. \tag{17}$$

**Theorem 2.** Suppose that multi-agent systems are composed of $n_1$ independent agents with $n_1$ followers and $n_2$ leaders, whose connection network topology is undirected with Assumption 1. Then fractional-order multi-agent system (10) with time delays can asymptotically reach containment control, if

$$τ < \frac{(2 - α)π}{2(λ^*)^{1/α}}, \tag{18}$$

where $λ^* = \max\{λ_i, i \in Ω\}$, $λ_i$ is the eigenvalues of matrix $L_1$.

**Proof.** By applying Laplace transformation to system(17), we can obtain the characteristic equation of the system

$$\det(s^{α}I_n + γe^{-τs}L_1) = 0. \tag{19}$$

Since the Laplacian matrix $L_1$ is symmetrical positive definite, there is an orthogonal matrix $P$ satisfying $L_1 = PΛP^{-1}$, where $Λ = \text{diag}\{λ_1, ..., λ_n\}$ with $λ_1 > 0$. Therefore, the root of the characteristic equation is satisfied with $s \neq 0$.

When $s \neq 0$, let $F(s) = \det(I_n + γs^{-α}e^{-τs}L_1)$, we will prove that all solutions of $F(s) = 0$ have negative real
parts. Let \( G(s) = \gamma s^{-\alpha} e^{-\tau s} L_1 \), according to the generalized Nyquist criterion, if for \( s = j\omega \), where \( j \) is complex number unit, point \(-1 + j0\) is not surrounded by the Nyquist curve of \( G(j\omega) \)'s eigenvalues, then all zero points of \( F(s) \) have negative real parts. Let \( s = j\omega \), we can get

\[
G(j\omega) = \omega^{-\alpha} e^{-j((\omega+\alpha\pi/2)\gamma) L_1}.
\]

We have the eigenvalues of \( G(j\omega) \)

\[
|\lambda I - G(j\omega)| = |\lambda I - ((\omega^{-\alpha} e^{-j((\omega+\alpha\pi/2)\gamma) L_1})| = \prod_{i=1}^{n_1} (\lambda - \gamma \lambda_i^{-\alpha} e^{-j((\omega+\alpha\pi/2)\gamma)}),
\]

where \( \lambda_i \) is the eigenvalues of \( L_1 \). When \( \omega = (2 - \alpha)\pi/(2\tau) \) the Nyquist curve of \( G(j\omega) \)'s eigenvalues will cross the left of the real axis. If

\[
\tau < \min\{\frac{(2 - \alpha)\pi}{2(\lambda_i^{1/\alpha})}, i = 1, 2, \ldots n_1\},
\]

the point \(-1 + j0\) is not surrounded by the Nyquist curve of \( G(j\omega) \)'s eigenvalues. Since fractional order \( \alpha \in (0, 1] \), we obtain

\[
\tau < (2 - \alpha)\pi/(2(\hat{\lambda})^{1/\alpha}),
\]

where \( \hat{\lambda} = \max\{\lambda_i, i \in I\} \), the fractional-order multi-agent system (11) with time delays can asymptotically reach containment control.

**Corollary 1.** Suppose multi-agent systems are composed of \( n \) independent agents with \( n_2 = 1 \) leader, whose connection network topology is directed and symmetrical with Assumption 1. Then FOMAS (10) with time delays can asymptotically follow the tracks of the leader, if

\[
\tau < \frac{(2 - \alpha)\pi}{2(\lambda_{\max}^{1/\alpha})},
\]

where \( \lambda_{\max} \) is the max eigenvalue of matrix \( L_1 \).

**Corollary 2.** Suppose multi-agent systems are composed of \( n \) independent agents with \( n_1 \) followers and \( n_2 \) leaders, whose connection network topology is directed and symmetrical with Assumption 1. Then fractional order multi-agent system (10) with time delays can asymptotically reach consensus with \( \alpha = 1 \), if

\[
2\gamma\tau < \frac{\pi}{\lambda_{\max}},
\]

where \( \lambda_{\max} \) is the max eigenvalue of matrix \( L_1 \).

**Remark 4.** If the fractional order \( \alpha = 1 \) in FOMAS, the containment control result in Theorem 2 will become that of delayed multi-agent systems with integer-order dynamics.

**Remark 5.** The consensus result in Corollary 2 for \( \gamma = 1 \) is in accord with that of delayed multi-agent systems with integer-order dynamics in [2].

V. SIMULATIONS

Consider the dynamic topology with 5 followers and 3 leaders (illustrated as A1, A2, A3) shown in Fig. 1, where the connection weights of each edge is 1. Suppose the fractional order of the multi-agent system \( \alpha = 0.9 \).

From the communication topology of FOMAS, the system matrix can be obtained,

\[
L_1 = \begin{bmatrix}
3 & -1 & 0 & 0 & -1 \\
-1 & 2 & 0 & 0 & 0 \\
0 & 0 & 2 & -1 & 0 \\
0 & 0 & -1 & 3 & -1 \\
-1 & 0 & 0 & 1 & 3
\end{bmatrix}
\]

Fig. 1. Network topology of multi-agent systems.

Assume that the control parameter of system is taken \( \gamma = 1.0 \). The initial positions of followers are taken as \( x_1(0) = (1, 1), \ x_2(0) = (1, 2), \ x_3(0) = (2, 1), \ x_4(0) = (2, 3), \ x_5(0) = (3, 2) \), respectively. The initial positions of leaders are taken as \( A_1(0) = (4, 4), \ A_2(0) = (4, 6), \ A_3(0) = (6, 4) \). Fig. 2 shows the state trajectories of FOMAS without time delays, where the followers have converged into the convex hull formed by the leaders.

Fig. 2. Moving track of FOMAS without communication delays.
Next, we will verify the results of FOMAS with time delays. The maximum eigenvalue of $L_1$ is 4.618. According to the constraints of Theorem 2 in this paper, the allowed upper bound of the delays is 0.3157. Let $\tau(t) = 0.20$ is the time delay of multi-agent systems. The initial parameters in the experiments are same as the simulation without time delays. Fig. 3 shows the state trajectories of FOMAS with time delays, where the followers have converged into the convex hull formed by the leaders.

![Fig. 3. Moving track of FOMAS with communication delay $\tau = 0.20$.](image)

Then, we will enlarge the time delays in FOMAS. Let $\tau(t) = 0.30$ is the time delay of multi-agent systems in the experiments. Fig. 4 shows the running trajectories of FOMAS. The followers can asymptotically converge to the dynamic region formed by three leaders, i.e., the containment control of fractional-order multi-agent systems with time delays can be achieved.

![Fig. 4. Moving track of FOMAS with communication delay $\tau = 0.30$.](image)

**VI. CONCLUSION**

This paper studies containment control of fractional multi-agent systems with communication time delays. Containment consensus of multi-agent systems with directed network topology is studied. By applying the stability theory of frequency domain, FOMAS with delay is analyzed, and the relationship between the control gain of multi-agent systems and the upper bound of time delays is derived. Suppose the orders of the fractional dynamical systems are all $1$, the extended conclusion in this paper is the same with ordinary integer order systems. The containment control of fractional order multi-agent systems with dynamical topologies and linear time-varying (LTV) systems will be investigated in the future works.

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